

## Note on a Model of Chinese National Income Determination\*

A macroeconomic model of Chow (1985) explaining aggregate consumption by the permanent income hypothesis of Robert Hall and aggregate investment by the accelerations principle was found to fit Chinese annual data from 1952 to 1982 well. This note shows that the same model can successfully explain Chinese annual data from 1978 to 2006.

The model of Chow (1985) starts with the national income identity  $Y_t = C_t + I_t$  where  $Y_t$ ,  $C_t$ , and  $I_t$  denote respectively national income, consumption and investment in year  $t$  in constant prices.  $X_t = \text{exports} - \text{imports}$  is omitted as a component of  $Y_t$ , because during the sample period 1952–1982 this variable is less than half of one percent of  $Y$ , except for 1982 when it equals 1.6%.

Consumption  $C$  is determined by the permanent income hypothesis of Hall (1978), namely, as a random walk with drift. To determine investment  $I$  assume that desired capital stock  $K^*$  equals a constant plus  $aY$ , and that actual change in capital stock  $K_t - K_{t-1}$  equals a fraction  $b$  of the desired change in capital stock or  $b(K_t^* - K_{t-1})$ . Substituting the linear function of  $Y$  for  $K^*$  in this equation and solving for  $K_t$  give  $K_t = \text{const.} + abY_t + (1 - b)K_{t-1}$ . Since gross investment  $I_t$  is defined as  $K_t - (1 - d)K_{t-1}$  where  $d$  is the annual rate of depreciation, we can subtract  $(1 - d)$  times the

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equation for  $K_{t-1}$  from the above equation for  $K_t$  to obtain an equation for investment

$$I_t = K_t - (1 - d) K_{t-1} = \text{const.} + ab[Y_t - (1 - d)Y_{t-1}] + (1 - b)I_{t-1}.$$

Given a small rate of depreciation which is equal to about 0.04 for the capital stock in China, investment  $I_t$  depends on the rate of change in output  $Y$  according to the accelerations principle.

I have estimated this same model using Chinese data from 1978 to 2006. Data on  $Y = \text{GDP}$ ,  $C$ ,  $I$  and  $X = \text{exports} - \text{imports}$  (measured in 100 million RMB) in nominal terms are presented in Table 1. To obtain these variables in constant prices I have divided them by a price index. The price index, also presented in Table 1, is the ratio of  $Y$  in nominal terms to  $Y$  in real terms. The consumption and investment equations are estimated by the method of two-stage least squares. In the first stage  $Y_t$  is estimated by a regression on  $C_{t-1}$ ,  $I_{t-1}$ ,  $X_t$  and  $X_{t-1}$  to yield, with  $X$  assumed to be exogenous,

$$\begin{aligned} Y_t^* &= 140.8(116.4) + 0.8841(0.0604)C_{t-1} + 1.4254(0.0951)I_{t-1} \\ &\quad - 0.4815(0.2616)X_t + 1.4073(0.2883)X_{t-1} \\ R^2 &= 0.9996; s = 273.4. \end{aligned} \quad (1)$$

The number in parentheses after each coefficient is its standard error. The variables are measured in 100 million RMB in 1978 prices, with the price index in 2006 equal to 4.598 as shown in Table 1.

In the second stage of two-stage least squares I have estimated the consumption function

$$\begin{aligned} C_t &= 218.86 + 1.067(0.074) C_{t-1} - 0.0051(0.0371)Y_t^* \\ R^2 &= 0.9985; s = 271.24. \end{aligned} \quad (2a)$$

This result confirms the permanent income hypothesis of Hall perfectly since the coefficient of  $C_{t-1}$  is almost exactly 1 and the coefficient of income  $Y$  is almost equal to 0. Given the result (2a) I have dropped the variable  $Y_t^*$  and re-estimated the consumption function to obtain

$$\begin{aligned} C_t &= 226.05(91.78) + 1.0570(0.0079) C_{t-1} \\ R^2 &= 0.9985; s = 266.08. \end{aligned} \quad (2)$$

Table 1. Data on China's National Income and Its Determinants

Year	Y	C	I	X	P
1978	3605.6	2239.1	1377.9	-11.4	1
1979	4092.6	2633.7	1478.9	-20	1.054896
1980	4592.9	3007.9	1599.7	-14.7	1.098124
1981	5008.8	3361.5	1630.2	17.1	1.137733
1982	5590	3714.8	1784.2	91	1.164813
1983	6216.2	4126.4	2039	50.8	1.168049
1984	7362.7	4846.3	2515.1	1.3	1.201187
1985	9076.7	5986.3	3457.5	-367.1	1.305023
1986	10508.5	6821.8	3941.9	-255.2	1.387854
1987	12277.4	7804.6	4462	10.8	1.453304
1988	15388.6	9839.5	5700.2	-151.1	1.63712
1989	17311.3	11164.2	6332.7	-185.6	1.769711
1990	19347.8	12090.5	6747	510.3	1.904878
1991	22577.4	14091.9	7868	617.5	2.035682
1992	27565.2	17203.3	10086.3	275.6	2.175614
1993	36938.1	21899.9	15717.7	-679.5	2.558603
1994	50217.4	29242.2	20341.1	634.1	3.075886
1995	63216.9	36748.2	25470.1	998.6	3.490539
1996	74163.6	43919.5	28784.9	1459.2	3.722223
1997	81658.5	48140.6	29968	3549.9	3.750238
1998	86531.6	51588.2	31314.2	3629.2	3.685385
1999	91125	55636.9	32951.5	2536.6	3.605819
2000	98749	61516	34842.8	2390.2	3.604115
2001	108972.4	66878.3	39769.4	2324.7	3.672308
2002	120350.3	71691.2	45565	3094.1	3.717834
2003	136398.8	77449.5	55963	2986.3	3.829693
2004	160280.4	87032.9	69168.4	4079.1	4.088025
2005	188692.1	97822.7	80646.3	10223.1	4.358183
2006	221170.5	110413.2	94103.2	16654.1	4.598263

Sources: Y = GDP, C = Consumption, I = Investment, X = exports - imports in nominal terms, measured in 100 million RMB, are found in Tables 3-15 of *China Statistical Yearbook 2007*. The price index P is the ratio of Y in nominal terms and Y in real terms, the latter given in Tables 3 and 4 of *China Statistical Yearbook 2007*.

The investment function is

$$I_t = -399.04(139.79) + 2.4149(0.6470) Y_t^* - 2.2861(0.6281) Y_{t-1} + 0.2233(0.2369) I_{t-1}$$

$$R^2 = 0.9968; s = 327.4. \quad (3a)$$

Note that the coefficient of  $Y_{t-1}$  is opposite in sign and slightly less in magnitude (because of the rate of depreciation) to the coefficient of  $Y_t^*$ . This confirms the accelerations principle that investment depends on the rate of change in income.

Given the coefficients of  $Y_t^*$  and  $Y_{t-1}$  in Eq. (3a) to be almost equal in magnitude I replace these variables by the variable  $(Y_t^* - Y_{t-1})$  to obtain the investment function

$$I_t = -186.23(120.84) + 1.7782(0.6513)(Y_t^* - Y_{t-1}) + 0.6866(0.1589) I_{t-1}$$

$$R^2 = 0.9960; s = 359.28. \quad (3)$$

In Chow (1985) I reported results similar to Eqs. (2) and (3) obtained by using Chinese annual data from 1952 to 1982. In the consumption function the coefficient of lagged consumption was almost equal to 1 and the coefficient of income was 0. In the investment equation the coefficient of  $Y_{t-1}$  was negative and slightly less in magnitude than the coefficient of  $Y$  and I replaced these variables by their difference as in Eq. (3). The results showed that the coefficient of this difference in the investment equation was smaller than 1.7782 possibly because the ratio  $a$  of capital stock to output was smaller and the adjustment coefficient  $b$  for capital stock to reach equilibrium was also smaller before 1978.

In conclusion I have found that the permanent income hypothesis of Hall (1978) to explain consumption and the accelerations principle to explain investment are well supported by Chinese macro data for the periods 1952–1982 and 1987–2006 as well. This is one example of the applicability of economic theory to the Chinese economy. Other examples can be found in Chow (2007).

## References

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