



Revisiting the empirics of inflation in China: A smooth transition error correction approach

Lingxiang Zhang

School of Management and Economics, Beijing Institute of Technology, Beijing, Haidian district, 100081, People's Republic of China

ARTICLE INFO

Article history:

Received 20 July 2012

Received in revised form

21 December 2012

Accepted 16 January 2013

Available online 29 January 2013

JEL classification:

C22

E31

E52

Keywords:

Inflation

China

Smooth transition error correction

ABSTRACT

Using the same data as Chow and Wang (2010) [Chow, Gregory C., Wang, Peng, 2010. The empirics of inflation in China. *Economics Letters* 109, 28–30], as well as a smooth transition regression model, this paper reconsiders the empirics of inflation in China. The estimated smooth transition error correction model indicates the significant regime-switching behavior of inflation in China, in contrast to the results derived with Chow and Wang's model of constant parameters.

© 2013 Elsevier B.V. All rights reserved.

1. Introduction

On the basis of the classical quantity theory of money, Chow (1987) estimates a residual-based error correction model proposed by Granger and Engle (1987) to explain inflation in China. Chow and Wang (2010) update the aforementioned model by using 1952 to 2008 data. The estimated model shows that the parameters remain constant. However, when we reexamine the linear model of Chow and Wang (2010), we find strong evidence that shows some form of misspecification, which makes us doubt whether the linear model adequately describes the empirics of inflation in China. Therefore, considering nonlinearity is promising in explaining the inflation in China.

This paper aims to reconsider the empirics of inflation in China by using a smooth transition error mechanism. Results show that the inflation dynamics in China have significant regime-switching characteristics, and that the estimated smooth transition error correction model exhibits better fit than the linear model.

2. Nonlinear unit root tests

We use the same variables and data as those employed by Chow and Wang (2010). For simplicity, we define $p = \log(P)$,

$m = \log(M2/Y)$, where P is the retail price index, $M2$ is the money supply, and Y is the real GDP index.

The Augmented Dickey–Fuller tests strongly suggest the presence of a unit root in p and m . However, simulation studies by Balke and Fomby (1997) and Taylor et al. (2001) show that, the power of conventional unit root tests can be dramatically low when tested against nonlinear alternatives. Recently, Kapetanios et al. (2003), Park and Shintani (2005), and Kiliç (2011) proposed nonlinear unit root tests (denoted by t_{NL} , $inf-t$, and t_{ESTAR} , respectively) based on a smooth transition autoregressive model.¹

Table 1 presents the results of the three nonlinear unit root tests mentioned above. All the three tests reject the unit root null at the 10% level, but for the $inf-t$ and t_{ESTAR} tests, the results are more significant for both the p_t and m_t series. We therefore believe that these two series are global stationary processes.

3. Reconsidering the error-correction mechanism

Given that p and m are global stationary, we can directly regress p on m and on other deterministic terms without performing a cointegration test; an error correction model can also be derived on the basis of this regression. Nevertheless, the estimated

¹ For the details about the three tests, the readers are directed to the related references.

E-mail address: lingxiangzh@163.com.

Table 1
Nonlinear unit root tests for the inflation rate in China and money supply-to-output ratio.

Test	p_t			m_t		
	Statistic value	Lag length	Transition variable	Statistic value	Lag length	Transition variable
inf- t	-3.779**	9	Δp_{t-4}	-8.536***	9	Δm_{t-4}
t_{NL}	-3.370*	9	p_{t-4}	-3.925**	9	m_{t-2}
t_{ESTAR}	-2.642**	1	Δp_{t-2}	-2.662**	10	Δm_{t-2}

Notes: We follow [Caner and Hansen \(2001\)](#) and select a transition variable that minimizes the residual sum of squares of corresponding regressions. Lag lengths are selected by using BIC. The 1%, 5%, and 10% critical values for the inf- t test are -3.99, -3.45, and -3.16, respectively. Those for the t_{NL} test are -3.93, -3.40, and -3.13, respectively, and those for the t_{ESTAR} test are -3.19, -2.57, and -2.23, respectively.

*** Denote significance at the 1% level.
** Denote significance at the 5% level.
* Denote significance at the 10% level.

cointegrating equation and the error correction equation used by [Chow and Wang \(2010\)](#) are still available. This estimate is determined by a direct regression of p on a constant m and on structural break dummy variables in level and slope.²

Therefore, we construct the linear baseline model according to the last equation used by [Chow and Wang \(2010\)](#):

$$\Delta p_t = -0.0015 + 0.6044\Delta p_{t-1} + 0.1633\Delta m_t - 0.2429u_{t-1} + \hat{\varepsilon}_t(0.0053) \quad (0.0846) \quad (0.0373) \quad (0.0591), \quad (1)$$

$$\bar{R}^2 = 0.66, \quad \hat{\sigma}_t = 0.031, \quad pJB = 0.001,$$

$$pLM_{ARCH}(1) = 0.647, \quad pLM_{ARCH}(4) = 0.046,$$

$$pLM_{AR}(1) = 0.435, \quad pLM_{AR}(4) = 0.375,$$

$$pLM_{RESET}(1) = 0.011$$

where u_t denotes the error correction term and $\hat{\sigma}_t$ is the residual standard deviation. Furthermore, the figures in parentheses below the parameter estimates are estimated standard deviations. Misspecification tests are also conducted for model evaluation.³ The JB test rejects normality, and the p -value of the McLeod–Li statistic shows heteroskedasticity in the residual at the 5% significant level when the maximum lag in the statistic is 4. Moreover, the RESET result shows that the linear error correction model is inadequate for predicting inflation in China. These outcomes may be interpreted as evidence of nonlinearity. Therefore, the next step is to test linearity against smooth transition regression (STR) nonlinearity.

Here, we introduce the specification test only briefly. As for the modeling cycle and corresponding tests of the STR model, interested readers are referred to [Teräsvirta \(1994\)](#), [van Dijk et al. \(2002\)](#), and [Teräsvirta et al. \(2010\)](#). Consider the following logistic STR model (LSTR):

$$y_t = \theta'_1 x_t + \theta'_2 x_t (1 + \exp\{-\gamma(s_t - c)\})^{-1} + \varepsilon_t, \quad (2)$$

where $x_t = (1, y_{t-1}, \dots, y_{t-p}, x_{1t}, \dots, x_{kt})'$; γ is the transition speed coefficient; c is the threshold value; and s_t represents the transition variable. A Taylor series approximation about $\gamma = 0$ is used and the tests are based on the following transformed equation:

$$y_t = \beta'_0 x_t + \beta'_1 x_t s_t + \beta'_2 x_t s_t^2 + \beta'_3 x_t s_t^3 + e_t, \quad (3)$$

where $\beta_i, i = 0, \dots, 3$ are the reparameterized coefficient vectors; hence, the null hypothesis of linearity test corresponds to $H_0 : \beta_1 = \beta_2 = \beta_3 = 0$, which can be tested using the Lagrange multiplier (LM) test statistic with a standard asymptotic χ^2 -distribution. In small samples, using the F -version of the LM test statistic is a good strategy because it has a better size. Furthermore, [Teräsvirta \(1994\)](#) suggests computing this LM statistic for various candidate transition variables s_{1t}, \dots, s_{mt} , say, and selecting the one for which the p -value of the test is the smallest.

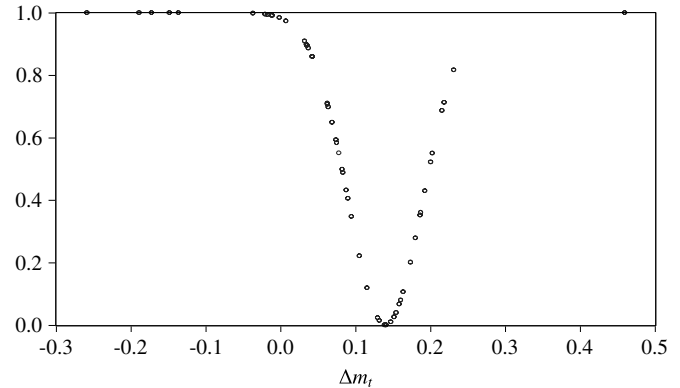


Fig. 1. Values of the transition function of estimated model (5). Each dot corresponds to an observation.

To select the appropriate form of the transition function, consider the sequence of the null hypotheses

$$H_{03} : \beta_3 = 0$$

$$H_{02} : \beta_2 = 0 | \beta_3 = 0$$

$$H_{01} : \beta_1 = 0 | \beta_2 = \beta_3 = 0$$

in Eq. (3), all of which can be tested by LM-type tests. [Teräsvirta \(1994\)](#) reexamine : if the p -value of the test that corresponds to H_{02} is the smallest, an exponential STR (ESTR) model should be selected; in all other cases, an LSTR model is the preferred choice.

[Escribano and Jordá \(1999\)](#) propose an alternative transition function selection procedure, which is based on the following auxiliary test equation:

$$y_t = \beta'_0 x_t + \beta'_1 x_t s_t + \beta'_2 x_t s_t^2 + \beta'_3 x_t s_t^3 + \beta'_4 x_t s_t^4 + e_t. \quad (4)$$

They suggest testing the hypotheses

$$H_{0E} : \beta_2 = \beta_4 = 0$$

$$H_{0L} : \beta_1 = \beta_3 = 0$$

in Eq. (4) and selecting an LSTR (ESTR) model if the minimum p -value is obtained for H_{0L} (H_{0E}).

On the basis of linear baseline model (1), we perform specification tests, whose p -values are shown in [Table 2](#). The table indicates that, linearity is rejected at the 5% significance level for $s_t = \Delta m_t, \Delta p_{t-1}, \Delta p_{t-2}$ and that Δm_t may be considered the transition variable because it presents the smallest corresponding p -value.

We find that ESTR is better not only in terms of goodness of fit, but also in terms of diagnostic test results. We therefore present only the results for this ESTR model. Following [van Dijk et al. \(2002\)](#), we retain the variables whose parameters have t -statistics that exceed 1 in absolute value. The smooth transition error correction model is estimated as

² Note that this equation does not have a cointegration interpretation as in [Chow and Wang \(2010\)](#).

³ These misspecification tests are not provided in [Chow and Wang \(2010\)](#).

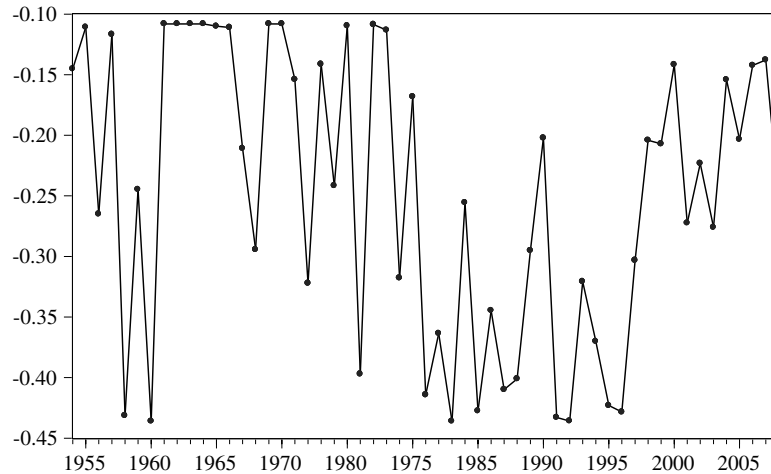


Fig. 2. Values of speed-of-adjustment parameter of the nonlinear error correction model.

Table 2
LM-type tests for STR nonlinearity and STR model selection.

Transition variable S_t	Teräsvirta				Escribano–Jordá	
	H_0	H_{03}	H_{02}	H_{01}	H_{0L}	H_{0E}
Δm_t	0.0013	0.0085	0.0335	0.0930	0.0004	0.0031
Δm_{t-1}	0.0796	0.1277	0.3454	0.0902	0.3612	0.5327
Δm_{t-2}	0.7395	0.9107	0.6368	0.2621	0.7346	0.9910
Δm_{t-3}	0.4009	0.4375	0.1021	0.9538	0.6973	1.0000
Δp_{t-1}	0.0102	0.0307	0.0729	0.1358	0.1633	0.0397
Δp_{t-2}	0.0138	0.1484	0.0061	0.4083	0.2922	0.5921
Δp_{t-3}	0.6292	0.7608	0.1326	0.9687	0.1697	0.3969
Δp_{t-4}	0.6207	0.3338	0.8110	0.4336	0.0904	0.0920
t	0.1370	0.1102	0.6296	0.1205	0.2810	0.2419

Notes: The p -values of the F -statistics of the LM-type tests are used in the specification procedures of Teräsvirta (1994) and Escribano and Jordá (1999). Hypotheses $H_0, H_{01}, H_{02}, H_{03}, H_{0L}$ and H_{0E} are discussed in Eqs. (3) and (4). Transition variable t denotes the deterministic time trend.

$$\begin{aligned} \Delta p_t = & -0.033 + 1.135 \Delta p_{t-1} + 0.164 \Delta m_t + 0.049 \Delta m_{t-1} - 0.436 u_{t-1} \\ & (0.014) \quad (0.194) \quad (0.038) \quad (0.045) \quad (0.114) \\ & + (0.040 - 0.956 \Delta p_{t-1} - 0.191 \Delta p_{t-2} + 0.328 u_{t-1}) \\ & (0.015) \quad (0.262) \quad (0.172) \quad (0.178) \\ & \times [1 - \exp\{-2.904 (\Delta m_t - 0.141)^2 / \hat{\sigma}_{\Delta m_t}^2\}] + \hat{\varepsilon}_t \end{aligned} \quad (5)$$

$$\begin{aligned} T = 55[1954 - 2008], \quad \bar{R}^2 = 0.75, \quad \hat{\sigma} = 0.027, \\ \hat{\sigma} / \hat{\sigma}_l = 0.875, \quad p_{JB} = 0.098, \\ pLM_{ARCH}(1) = 0.146, \quad pLM_{ARCH}(4) = 0.134, \\ pLM_{AR}(1) = 0.387, \quad pLM_{AR}(4) = 0.452, \end{aligned}$$

where $\hat{\sigma}_{\Delta m_t}^2$ is the sample variance of Δm_t , and $\hat{\sigma}$ and $\hat{\sigma}_l$ denote the residual standard deviation in the estimated ESTR model and model (1), respectively. The residual standard deviation of model (5) is 12.5% smaller than that of linear model (1), indicating that Eq. (5) exhibits better fit than does Eq. (1). The residual series of Eq. (5) appears normal, and the LM tests of no conditional heteroskedasticity do not cause any problems. The results of the diagnostic tests show that, no evidence exists for the remaining residual autocorrelation and remaining nonlinearity or time variation in the parameters, but for space reasons those results are not reported, which are available upon request.⁴

⁴ Note that the long-run equilibrium relation can also be nonlinear. However, this paper does not consider this case, because the related theory is not well developed.

The transition function of Eq. (5) as a function of transition variable Δm_t is depicted in Fig. 1, which shows that the transition between the two extreme regimes is smooth. Our model shows that the inflation dynamics in China have significant regime-switching characteristics.

Moreover, the values of the speed-of-adjustment parameter for each year are depicted in Fig. 2, which shows that the response of Δp_t to the previous period's deviation from long-run equilibrium is not constant, unlike the constant response (-0.2429) in the model of constant parameters of Chow and Wang (2010).

4. Conclusion

In this paper, we reconsider the empirics of inflation in China using the same data employed by Chow and Wang (2010). Using three nonlinear unit tests, we find that the inflation rate in China and the money supply-to-output ratio are global stationary. We specify and estimate a smooth transition error correction model, which more accurately fits the data than does the linear model. Our model also shows that the inflation dynamics in China have significant regime-switching characteristics, in contrast to the results derived with Chow and Wang's (2010) model of constant parameters.

The choice of nonlinearity is only one of the many potential alternatives. All other nonlinear specifications are not necessarily inferior to the STR model. We conclude, however, that in the application in this paper, STR-based specifications serve as a useful approach to reconsidering the inflation dynamics in China.

Acknowledgments

The research was funded by grants of the China Ministry of Education (No. 12YJC790268) and the Excellent Young Scholars Research Fund of Beijing Institute of Technology.

References

- Balke, N.S., Fomby, T.B., 1997. Threshold cointegration. *International Economic Review* 38, 627–645.
- Caner, M., Hansen, B.E., 2001. Threshold autoregression with a unit root. *Econometrica* 69, 1555–1596.
- Chow, Gregory C., 1987. Money and price level determination in China. *Journal of Comparative Economics* 11, 319–333.
- Chow, Gregory C., Wang, Peng, 2010. The empirics of inflation in China. *Economics Letters* 109, 28–30.
- Escribano, A., Jordá, O., 1999. Improved testing and specification of smooth transition regression models. In: Rothman, P. (Ed.), *Nonlinear Time Series Analysis of Economic and Financial Data*. Kluwer, Boston, pp. 289–319.

- Granger, C.W.J., Engle, R., 1987. Co-integration and error-correction: representation, estimation and testing. *Econometrica* 55, 251–276.
- Kapetanios, G., Shin, Y., Snell, A., 2003. Testing for a unit root in the nonlinear STAR framework. *Journal of Econometrics* 112, 359–379.
- Kiliç, R., 2011. Testing for a unit root in a stationary ESTAR process. *Econometric Reviews* 30, 274–302.
- Park, J.Y., Shintani, M., 2005. Testing for a unit root against transitional autoregressive models. Working paper No. 05010, Department of Economics, Vanderbilt University.
- Taylor, M.P., Peel, D.A., Sarno, L., 2001. Nonlinear mean-reversion in real exchange rates: toward a solution to the purchasing power parity puzzles. *International Economic Review* 42, 1015–1042.
- Teräsvirta, T., 1994. Specification, estimation, and evaluation of smooth transition autoregressive models. *Journal of the American Statistical Association* 89, 208–218.
- Teräsvirta, T., Tjøstheim, D., Granger, C.W.J., 2010. *Modelling Nonlinear Economic Time Series*. Oxford University Press, Oxford.
- van Dijk, D., Teräsvirta, T., Franses, P.H., 2002. Smooth transition autoregressive models—a survey of recent developments. *Econometric Reviews* 21, 1–47.